

Perfect vortex beams expressed as Laguerre-Gauss modes

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Introducción

We prove that perfect vortex beams (PVB)[1] form basis and can be expressed in terms of Laguerre-Gauss(LG)[2] modes and vice versa.

Desarrollo

From [1,4,5] we have:

$$\sum_{l=-\infty}^{\infty} \int_0^{2\pi} \int_0^{\infty} PVB_l \cdot PVB_l^* \cdot r dr d\theta = 1 \quad (1)$$

From [2] we have the expression of the LG modes:

$$LG_{lp}(x) = \sqrt{\frac{2}{\pi}} \sqrt{\frac{p!}{(|l|+n)!}} \frac{\exp^{-\frac{ikr^2}{2q(z)}}}{W(z)} \left[\frac{\sqrt{2}r}{W(z)} \right]^{|l|} L_p^{|l|} \left[\frac{2r^2}{W(z)^2} \right] \exp^{i(l\theta + (2p+|l|+1)\zeta(z))} \quad (2)$$

From [3] we can obtain the coefficients of expansion C_{lp} and C_l :

$$C_{lp} = \int_0^{2\pi} \int_0^{\infty} PVB_l \cdot LG_{lp}^* \cdot r dr d\theta \quad C_l = \int_0^{2\pi} \int_0^{\infty} PVB_l^* \cdot LG_{lp} \cdot r dr d\theta \quad (3)$$

With which we can write:

$$PVB_l = \sum_{p=0}^{\infty} \sum_{l=-\infty}^{\infty} C_{lp} \cdot LG_{lp} \quad LG_{lp} = \sum_{l=-\infty}^{\infty} \int_0^{\infty} C_l \cdot PVB_l \cdot r dr \quad (4)$$

Referencias

[1]Pravin Vaity and Leslie Rusch, Opt. Lett. 40, 597-600 (2015)

[2]Giuseppe Vallone, Opt. Lett. 40, 1717-1720 (2015)

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[4] George Arfken, Third edition, equation (11.111)

[5] I.S. Gradshteyn and I.M. Ryzhik, "Table of Integrals, Series, and Products", Seventh edition, equations 6.633-2 and 7.421-4