

# Hubble tension and matter inhomogeneities: A theoretical perspective

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## Introducción

We have studied how local density perturbations could reconcile the Hubble tension. We reproduced a local void through a perturbed FLRW metric with a potential  $\Phi$  which depends on both time and space. This method allowed us to obtain a perturbed luminosity distance, which is compared with both local and cosmological data. We got a region of local parameters,  $q_0^{Lo}$  and  $j_0^{Lo}$ , which are in agreement with a local void of  $\Omega_{m,void} = (-0,30 \pm 0,15)\Omega_m$  explaining the differences between the local  $H_0$  and the Planck  $H_0$ . However, when constraining local cosmological parameters with previous results, we found that neither  $\Lambda$ CDM nor  $\Lambda(\omega)$ CDM could solve the Hubble tension.

## Desarrollo

In a perturbed FLRW background by a potential  $\Phi(r, t)$ , the (perturbed) redshift of an emitted photon at time  $t_e$  and position  $r_e$  is given by[1]

$$z_e = \frac{a(t_0)}{a(t_e)} - 1$$

and

$$\delta z_e = \frac{a(t_0)}{a(t)} \left[ -\Phi(r_e \hat{n}, t_e) + \Phi(0, t_0) - 2 \int_{t_e}^{t_0} \left\{ \frac{\partial}{\partial t} \Phi(r \hat{n}, t) \right\}_{r=s(t)} dt - \frac{a(t_e)}{c} \partial_r v^N(r_e \hat{n}, t) \right]$$

where  $a(t)$  is the usual scale factor and  $v^N$  is the velocity potential of the light source. The luminosity distance is then:

$$d_L(z, \delta z) = (1 + z + \delta z)r + (1 + z) \left[ \frac{1}{2} (\Phi(r \hat{n}, t) - \Phi(0, t_0))r - \int_0^r \Phi(r \hat{n}, t_0) dr \right] + \mathcal{O}(\Phi^2).$$

This expression will be helpful to compare with respect to Planck data.

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## Referencias

[1] M. San Martín and C. Rubio, doi = 10.48550/ARXIV.2107.14377,