

Thermo-statistical analogues of Hamilton-Jacobi and Einstein field equations

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Abstract

Riemannian formulation of classical fluctuation theory [1] appears after imposing the principle of general covariance, which requires a reformulation of Einstein postulate of classical fluctuation theory and Ruppeiner geometry of thermodynamics. This proposal predicts thermo-statistical counterparts of Hamilton-Jacobi equation of classical mechanics:

$$-\frac{\partial}{\partial \tau} \mathcal{S}(x, \tau) = \frac{1}{2} w \left[-g^{ij}(x) \frac{\partial \mathcal{S}(x, \tau)}{\partial x^i} \frac{\partial \mathcal{S}(x, \tau)}{\partial x^j} + \ell^2(x|\bar{x}) \right]. \quad (1)$$

and Einstein field equations of general relativity:

$$R_{ij} - \frac{1}{2} g_{ij} R - \frac{1}{2\kappa} (d-2) g_{ij} = T_{ij}. \quad (2)$$

The first analogy leads to a Riemannian extension of Onsager-Machlup theory of non-equilibrium thermodynamics, whose mathematical apparatuses resemble the ones of classical and quantum mechanics. The second analogy suggests that general relativity is the deterministic limit of a certain *information geometry* defined on the spacetime. This viewpoint is highly motivated by the interpretation of *time measuring* as a process of *statistical inference*. The existing analogies between microphysics and macrophysics [2] are analyzed within recently proposed *complex time approach* [3] (micro-macro coexistence scenario). This analysis motivates the introduction of the local Lorentzian metric for the complex 5D spacetime $\mathbb{M}^5 \simeq \mathbb{C} \otimes \mathbb{R}^3$:

$$d\ell^2 = \varepsilon_P^2 \left[|dz|^2 - \left(\frac{1}{\hbar c} d\mathbf{x} \right)^2 \right] = \frac{\hbar c^5}{G} \left[\frac{1}{4\kappa^2} d\eta^2 + \frac{1}{\hbar^2} \left(dt^2 - \frac{1}{c^2} d\mathbf{x}^2 \right) \right], \quad (3)$$

which favors a *gravitational origin* of the observed *macroscopic irreversibility* instead of a *thermodynamic emergence of gravitation* [4]. Apparently, this connection seems to be closely related with other two (unsolved) fundamental problem of physics.

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Referencias

- [1] L. Velazquez, J. Phys. A: Math and Theo. **45**, 175002 (2012); ibid **46**, 345003 (2013)
- [2] L. Velazquez, Ann. Phys. **327**, 1682 (2012)
- [3] L. Velazquez, C. Jaynes, and M. Parker, (E-print) Submitted to Entropy (2022)
- [4] T. Jacobson, Phys. Rev. Lett. **116**, 201101 (2016)